

The Problem

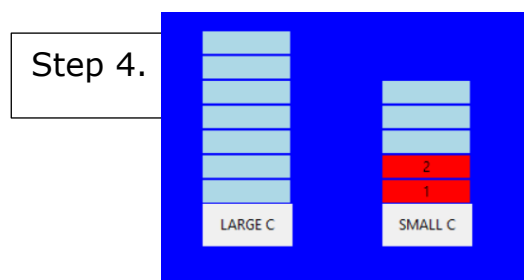
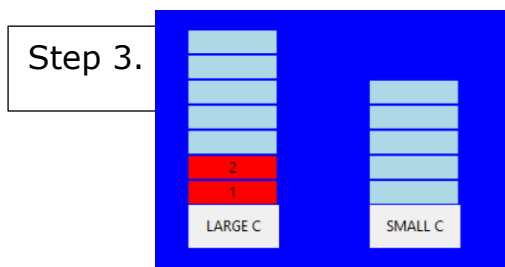
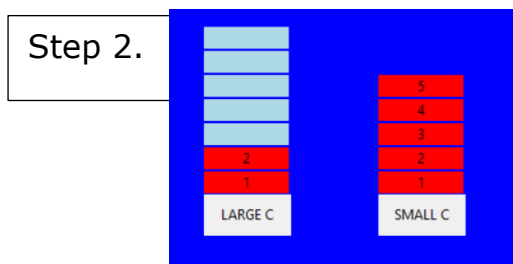
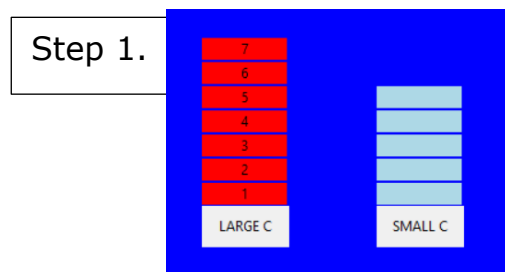
To measure out 4 litres from containers of 7l and 5l.

The 4 litres must be contained in the smaller container at the end of the process, and the larger one empty.

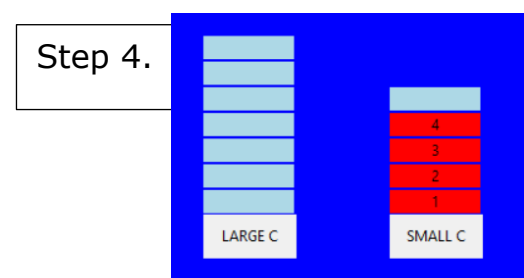
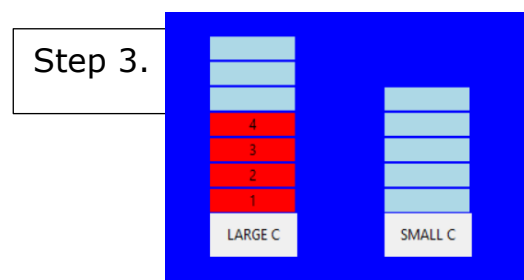
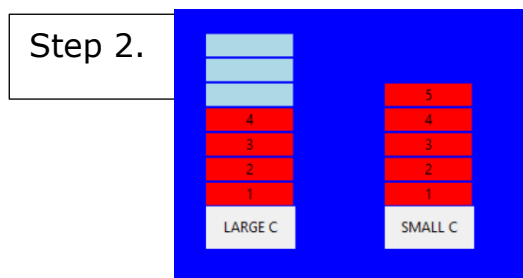
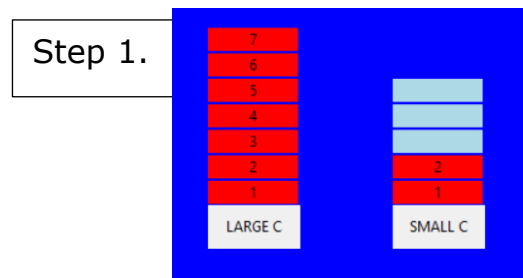
A Visual Solution

There are 4 steps involved to have 2 litres in the small container and an empty large container. The steps can be just repeated for a 4 litre solution.

First Iteration



Second Iteration



Solution in Words (very algorithmic)

The four steps can be described as follows :

1. Fill the larger container.
2. Pour the larger one into the smaller one, until the smaller container is full.
3. Empty the small one into a sink
4. Pour the difference from the larger into the smaller

Repeat steps 1-4. The larger container will be empty and the smaller one will contain 4 litres.

A more abstracted Mathematical Solution

If the equation $7x + 5y = 4$ has two integer solutions, then it is possible to measure out 4 litres.

Let's look at the volume of water in and out of the containers.

Briefly, let's say f is the number of fills of the large container and e is the number of empties into the sink (not pours into another container).

In the visual solution, $f = 2$ and $e = 0 \therefore x = 2$.

Let's say for the small container f' is the numbers of fills and e' the number of empties into the sink.

In the visual solution, $f' = 0$ and $e' = 2 \therefore y = -2$.

Substituting: $7(2) + 5(-2) = 4$ which means there must a solution for measuring 4 litres into a container.



Try these ones

Will the solution hold for 9 litre and 7 litre containers?

Will the steps work for any two containers as long the difference in their capacities is 2 litres?